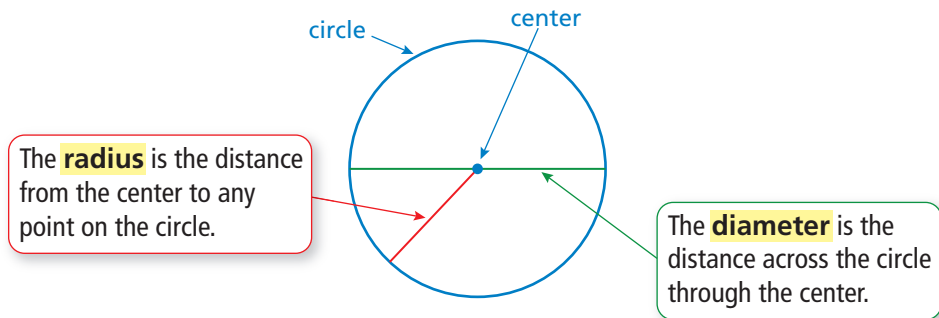


6.2b Circles

A **circle** is the set of all points in a plane that are the same distance from a point called the **center**.



Key Idea

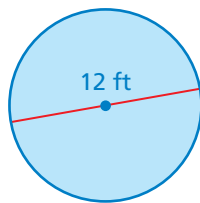
Radius and Diameter

Words The diameter d of a circle is twice the radius r . The radius r of a circle is one-half the diameter d .

Algebra Diameter: $d = 2r$ Radius: $r = \frac{d}{2}$

EXAMPLE 1 Finding a Radius and a Diameter

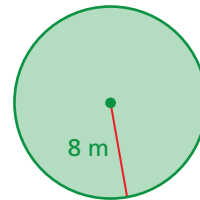
a. The diameter of a circle is 12 feet. Find the radius.



$$\begin{aligned} r &= \frac{d}{2} && \text{Radius of a circle} \\ &= \frac{12}{2} && \text{Substitute 12 for } d. \\ &= 6 && \text{Divide.} \end{aligned}$$

∴ The radius is 6 feet.

b. The radius of a circle is 8 meters. Find the diameter.



$$\begin{aligned} d &= 2r && \text{Diameter of a circle} \\ &= 2(8) && \text{Substitute 8 for } r. \\ &= 16 && \text{Multiply.} \end{aligned}$$

∴ The diameter is 16 meters.

Practice

- DIAMETER** The radius of a dartboard is 9 inches. Find the diameter.
- RADIUS** The diameter of a clock is 1 foot. Find the radius.

The distance around a circle is called the **circumference**. The ratio $\frac{\text{circumference}}{\text{diameter}}$ is the same for *every* circle and is represented by the Greek letter π , called **pi**. The value of π can be approximated as 3.14 or $\frac{22}{7}$.

Study Tip

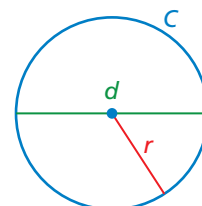
When the radius or diameter is a multiple of 7, it is easier to use $\frac{22}{7}$ as the estimate of π .

Key Ideas

Circumference of a Circle

Words The circumference C of a circle is equal to the product of π and the diameter d or the product of π and twice the radius r .

Algebra $C = \pi d$ or $C = 2\pi r$



Area of a Circle

Words The area A of a circle is the product of π and the square of the radius r .

Algebra $A = \pi r^2$

EXAMPLE 2 Finding the Circumference and Area of a Circle



Find (a) the circumference and (b) the area of the sticker. Use 3.14 for π .

a. $C = 2\pi r$

$\approx 2 \cdot 3.14 \cdot 3$ *Substitute.*

$= 6.28 \cdot 3$ *Simplify.*

$= 18.84$ *Simplify.*

∴ The circumference is about 18.84 centimeters.

b. $A = \pi r^2$

$\approx 3.14 \cdot (3)^2$

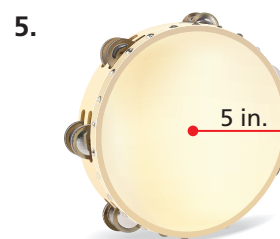
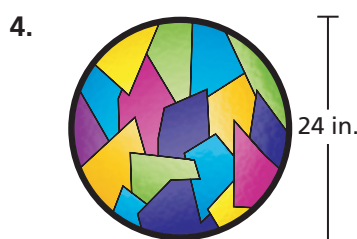
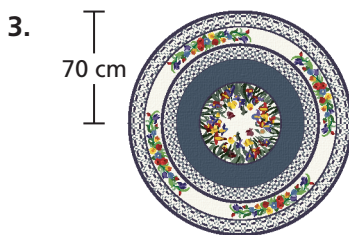
$= 3.14 \cdot 9$

$= 28.26$

∴ The area is about 28.26 square centimeters.

Practice

Find the circumference and area of the object. Use 3.14 or $\frac{22}{7}$ for π .



6. **TIRE** The diameter of a bicycle tire is 26 inches.

a. Find the circumference of the tire. Use 3.14 for π .

b. How many rotations does the tire make to travel 95 feet? Explain your reasoning.